

A LYAPUNOV–TYPE INEQUALITY FOR A FRACTIONAL BOUNDARY VALUE PROBLEM WITH CAPUTO–FABRIZIO DERIVATIVE

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Abstract. In this work we obtain a Lyapunov-type inequality for a fractional differential equation with Caputo-Fabrizio operator subject to Dirichlet-type boundary conditions. As an application, we obtain a lower bound for the eigenvalues of corresponding equations.

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