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L_p DUAL MIXED GEOMINIMAL SURFACE AREAS FOR MULTIPLE STAR BODIES

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Abstract. In this article, by defining L_p dual mixed quermassintegrals for multiple star bodies, we consider L_p dual mixed geominimal surface areas for multiple star bodies. Further, some related inequalities for this concept are obtained.

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