

ADDITIVE REFINEMENTS AND REVERSES OF YOUNG'S OPERATOR INEQUALITY WITH APPLICATIONS

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Abstract. In this paper we obtain some new additive refinements and reverses of Young's operator inequality. Applications related to the Hölder-McCarthy inequality for positive operators and for trace class operators on Hilbert spaces are given as well.

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