Journal of Mathematical Inequalities
Volume 13, Number 1 (2019), 275–286
doi:10.7153/jmi-2019-13-20

HYBRID ZIPF–MANDELBROT LAW

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Abstract. There is a unified approach, maximization of Shannon entropy, that naturally follows the path of generalization from Zipf's to hybrid Zipf's law. Extending this idea we make transition from Zipf-Mandelbrot to hybrid Zipf-Mandelbrot law. It is interesting that examination of its densities provides some new insights of Lerch's transcendent.

Mathematics subject classification (2010): 26D07, 26D15, 26D20, 26D99.
Keywords and phrases: Shannon entropy, Zipf-Mandelbrot law, log-convex functions, Chebyshev's inequality, Lyapunov's inequality, Lerch's transcendent.

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