

LYAPUNOV-TYPE INEQUALITIES FOR FRACTIONAL DIFFERENTIAL EQUATIONS UNDER MULTI-POINT BOUNDARY CONDITIONS

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Abstract. In this work, we establish new Lyapunov-type inequalities for fractional differential equations under multi-point boundary conditions.

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