

## MULTIDIMENSIONAL HARDY-TYPE INEQUALITIES ON TIME SCALES WITH VARIABLE EXPONENTS

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*Abstract.* A new Jensen inequality for multivariate superquadratic functions is derived and proved. The derived Jensen inequality is then employed to obtain the general Hardy-type integral inequality for superquadratic and subquadratic functions of several variables.

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