

REVERSE HILBERT TYPE INEQUALITIES

CHANG-JIAN ZHAO AND WING-SUM CHEUNG

Abstract. In this paper, some reverse Hilbert-Pachpatte's type inequalities involving series of nonnegative terms are established, which provide new estimates on inequality of this type.

Mathematics subject classification (2010): 26D15.

Keywords and phrases: Convex function, concave function, Jensen's inequality, Hilbert's inequality.

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