ON STATISTICALLY KÖTHE–TOEPLITZ DUALS

FATIH TEMIZSU AND MIKAIL ET

Abstract. In the present paper, we introduce the concept of Δ^m- statistical boundedness of real (or complex) numbers sequences by using generalized difference operator Δ^m and examine relationships between Δ^m- statistical convergence, Δ^m- statistical Cauchiness and Δ^m- statistical boundedness. In addition to that we compute the Köthe-Toeplitz and generalized Köthe-Toeplitz duals of the set of all Δ^m- statistical bounded sequences. Moreover, we come up with the idea of statistical α and β duals of the sets of sequence which makes us capable of creating statistical equivalents of the notions of normality and perfectness of sequence spaces.

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