SOME MULTIPLE INTEGRAL INEQUALITIES
VIA THE DIVERGENCE THEOREM

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Abstract. In this paper, by the use of the divergence theorem, we establish some inequalities for functions defined on closed and bounded subsets of the Euclidean space $\mathbb{R}^n$, $n \geqslant 2$.

Mathematics subject classification (2010): 26D15.

Keywords and phrases: Multiple integral inequalities, divergence theorem, Green identity, Gauss-Ostrogradsky identity.

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