

AN EIGENVALUE INEQUALITY FOR POSITIVE SEMIDEFINITE $k \times k$ BLOCK MATRICES

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Abstract. In this paper, we give some generalized results on matrix eigenvalue majorization inequality for positive semidefinite block matrices under a condition, which is a natural extended result given by Lin [4].

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