

## HERMITE–HADAMARD INEQUALITIES FOR CO–ORDINATED $\log -h$ –CONVEX FUNCTIONS

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**Abstract.** In this paper, we establish some Hermite–Hadamard type inequalities for co-ordinated  $\log -h$ -convex functions on rectangles from  $\mathbb{R}^n$ , which extend some known results. Some mappings connected with these inequalities and related results are also obtained.

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