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A NOTE ON TWO WEIGHTED DISCRETE CARLEMAN INEQUALITIES

BAOFENG LAI*, RUNQIU WANG AND HAO LIU

Abstract. In this paper, we re-examine two weighted discrete Carleman inequalities, discuss their correctness and optimal constants in detail, and get some correct and relatively complete conclusions.

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