

ON THE FURTHER REFINEMENT OF SOME OPERATOR INEQUALITIES FOR POSITIVE LINEAR MAP

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Abstract. In this paper, some further improvements of operator inequalities are given at the base of Yang et al.'s recent work [Filomat 32:12 (2018), 4333–4340] and [Math. Slovaca 69 (2019), 919–930] for positive linear map. Besides, the corresponding multiple-term refinements for scalars and operators are shown as well.

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