

A FRACTIONAL MAGNETIC HARDY–SOBOLEV INEQUALITY WITH TWO VARIABLES

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Abstract. A fractional magnetic Hardy-Sobolev inequality with two variables and critical exponents is considered in this paper, and the achievement to the best constant corresponding to this inequality is obtained.

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