ROUGH FRACTIONAL INTEGRAL
OPERATORS ON MORREY—ADAMS SPACES

DANIEL SALIM* AND WONO SETYA BUDHI

Abstract. In 1981, Adams introduced another variant of Morrey spaces, and we call it the Morrey–Adams space. In this paper, we investigate the boundedness of rough fractional integral operators on Morrey–Adams spaces under a weaker condition. We compare it with Adams' results. We then refine the results to vanishing Morrey–Adams spaces in the local sense. We also prove the beyond Adams' inequality of rough fractional integral operators on local Morrey–Adams spaces for the radial functions.

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