

SOME REFINEMENTS OF NUMERICAL RADIUS INEQUALITIES FOR 2×2 OPERATOR MATRICES

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Abstract. In this paper, new numerical radius inequalities for 2×2 operator matrices are proved. These numerical radius inequalities refine the existing upper bounds.

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