

## APPROXIMATION PROPERTIES OF GENERALIZED BLENDING TYPE LOTOTSKY–BERNSTEIN OPERATORS

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*Abstract.* In this paper, we introduce a family of blending type Bernstein operators  $L_n^{\alpha,s}(f;x)$  which depends on two parameters,  $\alpha$  and  $s$ . We prove a Korovkin type approximation theorem and obtain the rate of convergence of these operators. We also prove that these operators has monotonicity and convexity preserving properties for each  $\alpha$  and  $s$ . So far, Lototsky matrices that generates blending type Bernstein operators were ignored. In this paper, we also introduce Lototsky matrices that generates these new family of blending type Bernstein operators.

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