

## ESTIMATES FOR THE NUMERICAL RADIUS OF $n \times n$ OPERATOR MATRICES

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*Abstract.* We present new upper bounds for the numerical radius of  $n \times n$  operator matrices defined on a complex Hilbert space, i.e., operator matrices of the form  $[T_{ij}]$ , and illustrate with numerical examples that these bounds are better than the existing bounds.

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