

MATHEMATICAL INEQUALITIES ON SOME WEIGHTED MEANS

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Abstract. Some mathematical inequalities among various weighted means are studied. Inequalities on weighted logarithmic mean are given. Besides, the gap in Jensen's inequality is studied as a convex function approach. Consequently, some non-trivial inequalities on means are given. Some operator inequalities are also shown.

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