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REMARKS ON THE STABILITY OF THE 3–VARIABLE FUNCTIONAL INEQUALITIES OF DRYGAS

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Abstract. We give some remarks on the recent paper [*J. Math. Inequal.* **13** (4) (2019), 1235–1244]. Some misleading conclusions of their stability results are carefully discussed and corrected. Moreover, we reestablish their results with a more general assumption and a stronger conclusion.

Mathematics subject classification (2020): 39B05, 39B62, 39B82.
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