

## SHARP BOUND OF $m$ -LINEAR $n$ -DIMENSIONAL $p$ -ADIC HAUSDORFF OPERATORS ON $p$ -ADIC MORREY SPACES

XIRAN ZHANG, QIANJUN HE AND XIANG LI\*

**Abstract.** In this paper, we study the sharp bound for  $m$ -linear  $n$ -dimensional  $p$ -adic Hausdorff operators on central and noncentral  $p$ -adic Morrey spaces with power weights, and we also give the sharp bounds of  $p$ -adic Hausdorff operators on central and noncentral  $p$ -adic Morrey spaces. Moreover, this is a generalization of the previous results.

*Mathematics subject classification (2020):* Primary 42B25; Secondary 26D15.

*Keywords and phrases:* Sharp bound,  $p$ -adic Hausdorff operator,  $p$ -adic Morrey space, power weights.

### REFERENCES

- [1] S. ALBEVERIO AND W. KARWOSKI, *A random walk on  $p$ -adics: the generator and its spectrum*, Stochastic Process. Appl. **53** (1994), 1–22.
- [2] S. ALBEVERIO, A. YU. KHRENNIKOV AND M. SHELKOVICH, *Theory of  $p$ -adic distributions: linear and nonlinear models*, London Mathematical Lecture Note series, vol. 370, Cambridge University Press, Cambridge, 2010.
- [3] A. V. AVETISOV, A. H. BIKULOV, S. V. KOZYREV AND V. A. OSIPOV,  *$p$ -adic models of ultrametric diffusion constrained by hierarchical energy landscapes*, J. Phys. A: Math. Gen. **35** (2002), 177–189.
- [4] T. BATBLOD AND Y. SAWANO, *Sharp bounds for  $m$ -linear Hilbert-type operators on the weighted Morrey spaces*, Math. Inequal. Appl. **20** (1) (2017), 263–283.
- [5] Á. BÉNYI AND C. T. OH, *Best constants for certain multilinear integral operators*, J. Inequal. Appl. **2006** (2006), 1–12.
- [6] Y. DENG, D. YAN AND M. WEI, *Sharp estimates for  $m$ -linear  $p$ -adic Hardy and Hardy-Littlewood-Pólya operators on  $p$ -adic central Morrey spaces*, preprint, 2021.
- [7] G. L. GAO, X. M. WU AND W. C. GUO, *Some results for Hausdorff operators*, Math. Ineq. Appl. **18** (1) (2015), 155–168.
- [8] G. H. HARDY, J. E. LITTLEWOOD AND G. PÓLYA, *Inequalities*, Cambridge University Press, Cambridge, 1952.
- [9] Q. J. HE, M. Q. WEI AND D. Y. YAN, *Characterizations of  $p$ -adic central Campanato spaces via commutator of  $p$ -adic Hardy type operators*, J. Korean Math. Soc. **56** (3) (2019), 767–787.
- [10] Q. J. HE, M. Q. WEI AND D. Y. YAN, *Sharp bound for generalized  $m$ -linear  $n$ -dimensional Hardy-Littlewood-Pólya operator*, Anal. Theory Appl., **39**, (2023), 28–41.
- [11] A. KHRENNIKOV,  *$p$ -adic valued distributions in mathematical physics*, Kluwer, Dordrecht, 1994.
- [12] A. KHRENNIKOV, *Non-Archimedean analysis: Quantum Paradoxes, Dynamical Systems and Biological Models*, Kluwer, Dordrecht, 1997.
- [13] Y. C. KIM, *Carleson measures and the BMO space on the  $p$ -adic vector space*, Math. Nachr. **282** (9) (2009), 1278–1304.
- [14] Y. C. KIM, *Weak type estimates of square functions associated with quasiradial Bochner-Riesz means on certain Hardy spaces*, J. Math. Anal. Appl. **339** (1) (2008), 266–280.
- [15] X. LI, X. R. ZHANG AND Q. J. HE, *Sharp bounds for generalized  $m$ -linear  $n$ -dimensional  $p$ -adic Hardy-Littlewood-Pólya operator*, J. Funct. Spaces, 2021, Article ID 5366843, 8 pages.
- [16] K. S. RIM AND J. LEE, *Estimate of weighted Hard-Littlewood averages on the  $p$ -adic vector space*, J. Math. Anal. Appl. **324** (2006), 1470–1477.

- [17] K. M. ROGERS, *A van der Corput lemma for the  $p$ -adic numbers*, Proc. Amer. Math. Soc. **133** (12) (2005), 3525–3534.
- [18] K. M. ROGERS, *Maximal averages along curves over the  $p$ -adic numbers*, Bull. Austral. Math. Soc. **70** (3) (2004), 357–375.
- [19] S. G SHI, Z. W. FU AND S. Z. LU, *On the compactness of commutators of Hardy operators*, Pacific J. Math., **307** (2020), 239–256.
- [20] M. H. TAIBLESON, *Fourier analysis on local fields*, Princeton University Press, Princeton, 1975.
- [21] V. S. VARADARAJAN, *Path integrals for a class of  $p$ -adic Schrödinger equations*, Lett. Math. Phys. **39** (1997), 97–106.
- [22] V. S. VLADIMIRON, I. V. VOLOVICH, E. I. ZELENOV,  *$p$ -adic Analysis and Mathematical Physics*, Series on Soviet and East European Mathematics, vol. I, World Scientific, Singapore, 1992.
- [23] Q. Y. WU AND Z. W. FU, *Sharp estimates of  $m$ -linear  $p$ -adic Hardy and Hardy-Littlewood-Pólya operators*, J. Appl. Math. **2011** (2011), 1–20.
- [24] X. M. WU, G. L. GAO AND X. YU, *The boundedness of Hausdorff operators on Campanato spaces*, Acta Math. Sin. (Chin. Ser.) **57** (1) (2014), 1–8.
- [25] X. S. ZHANG, M. Q. WEI AND D. Y. YAN, *Sharp bounds of Hausdorff operators on Morrey spaces with power weights*, J. Univ. Chinese Academy Sci., **38** (5) (2021), 577–582.