

HYERS-ULAM TYPE STABILITY OF JENSEN OPERATORS IN LOCALLY CONVEX CONES

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Abstract. In the theory of locally convex cones, some methods are rather technical. This is the consequence of including infinity-type unbounded elements and the general non-availability of the cancellation law. In this paper, we consider the Hyers-Ulam stability problem in locally convex cones and prove the stability of Jensen operators in locally convex cones.

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