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A WEIGHTED WELCH INEQUALITY

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Abstract. In this paper, we give a generalization of the Welch inequality, a weighted version in the presence of a normal matrix as a weight. Also, we obtain connections with tight frames and we give some examples.

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