APPROXIMATE ADDITIVE (ρ_1, ρ_2)–RANDOM OPERATOR INEQUALITY IN MENGER BANACH SPACES

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Abstract. In this paper, we attempt to solve an additive (ρ_1, ρ_2)-random operator inequality. We also obtain the Hyers-Ulam stability of such random operator inequality in Menger Banach spaces by using two different approaches.

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