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NEW PROOFS ON TWO RECENT INEQUALITIES RELATED TO THE SPECTRAL NORM

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Abstract. Afraz et al. [1] recently obtained some norm inequalities involving a special class of functions for sector matrices. In this short note, we give alternative proofs of Afraz et al.'s two results [1] under the spectral norm.

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