

NEW L^q INEQUALITIES FOR POLYNOMIALS

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Abstract. In this paper we establish some new L^q inequalities for polynomials which generalize and refine some results of Szegő, Zygmund, De Bruijn and others.

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