

A GENERALIZATION OF PÓLYA'S INEQUALITY TO STOLARSKY AND GINI MEANS

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Abstract. Pólya's inequality has recently been extended in a general way involving two geometric means. We show that further extensions to Stolarsky and Gini means are possible. The two occurrences of the mean in each inequality can involve different parameters. Corresponding discrete results are also derived.

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