

A BEST POSSIBLE HADAMARD INEQUALITY

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Abstract. The classical Hadamard-Hermite inequality requires that the measure be a symmetric and positive. We prove versions which require neither of these conditions. Furthermore, we prove that no such theorems exist with less restrictions than ours, ie. they are best possible.

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