

THE JENSEN–STEFFENSEN INEQUALITY

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Abstract. In this paper a simple calculus proof is given of the Jensen-Steffensen inequality, and of an inverse inequality due to Pečarić.

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