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AN ENERGY—TYPE INEQUALITY

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Abstract. In this paper we will prove an Energy-Type inequality for the mild solution of the linear evolution equation. And for showing the strength and power of this inequality we will use this inequality to show continuity of the solution with respect to a parameter of the semilinear evolution equation with monotone nonlinearity.

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