

INEQUALITIES FOR A POLYNOMIAL AND ITS DERIVATIVE

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Abstract. Let $P(z)$ be a polynomial of degree n and $P'(z)$ its derivative. In this paper we shall obtain certain sharp generalization of some results of Govil, Malik and P. Turán concerning the maximum modulus of $P(z)$ and $P'(z)$.

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