

ON HEINZ–KATO TYPE CHARACTERIZATIONS OF THE FURUTA INEQUALITY II

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Abstract. This paper is a continuation of the previous one [8]. Here we show that it is still possible to have several characterizations of the Furuta inequality in terms of different types of the Heinz-Kato inequality. Some application are given.

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