

STOLARSKY–TOBEY MEAN IN n VARIABLES

J. PEČARIĆ AND V. ŠIMIĆ

Abstract. In this paper, an n -dimensional weighted Stolarsky–Tobey mean is defined via measure. This mean includes as special cases various generalizations of the logarithmic mean. Some elementary properties are listed and various inequalities derived. Attention is given to the case when the mean is specialized to Dirichlet measure. Relations to hypergeometric function are exhibited. An explicit form is given for the mean in the special case when all variables have equal weights.

Mathematics subject classification (1991): 26D15.

Key words and phrases: logarithmic mean, Stolarsky–Tobey mean, inequality, Dirichlet measure, hypergeometric function, convex functions.

REFERENCES

- [1] H. Alzer, *Über eine einparametrische Familie von Mittelwerten I*, Sitzungsber. Bayer. Akad. Wiss., mat.-naturw. Kl. (1987), 1-9.
- [2] H. Alzer, *Über eine einparametrische Familie von Mittelwerten II*, Sitzungsber. Bayer. Akad. Wiss., mat.-naturw. Kl. (1988), 23-39.
- [3] B. C. Carlson, *A hypergeometric mean value*, Proc. Amer. Math. Soc. **16** (1965), 759-766.
- [4] B. C. Carlson, *The logarithmic mean*, Amer. Math. Monthly **79** (1972), 615-618.
- [5] B. C. Carlson, *Special Functions of Applied Mathematics*, Academic Press, New York, 1977.
- [6] G. H. Hardy, J. E. Littlewood and G. Polya, *Inequalities*, 2nd.ed., Cambridge Univer. Press, Cambridge, 1959.
- [7] E. Neuman, *Inequalities involving multivariate convex functions, II*, Proc. Amer. Math. Soc. **109** (1990), 965-974.
- [8] E. Neuman, *The weighted logarithmic mean*, J. Math. Anal. Appl. **188** (1994), 885-900.
- [9] C. E. Pearce, J. Pečarić, V. Šimić, *On weighted generalized logarithmic means*, Houston J. of Math., **24** (1998), 459-465.
- [10] C. E. Pearce, J. Pečarić, V. Šimić, *Stolarsky Means and Hadamard's Inequality*, J. Math. Anal. Appl. **220** (1998), 99-109.
- [11] A. O. Pittenger, *The logarithmic mean in n variables*, Amer. Math. Monthly **92** (1987), 282-291.
- [12] K. B. Stolarsky, *Generalizations of the logarithmic mean*, Math. Mag. **48** (1975), 87-92.
- [13] M. D. Tobey, *Two-parameter Homogeneous Mean Value*, Proc. Amer. Math. Soc. **18** (1967), 9-14.