

SIMPLIFIED PROOF OF TANAHASHI'S RESULT ON THE BEST POSSIBILITY OF GENERALIZED FURUTA INEQUALITY

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Abstract. We give a simplified proof of Tanahashi's result on the best possibility of generalized Furuta inequality by using Tanahashi's result on the best possibility of Furuta inequality.

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