A NEW REFINEMENT OF THE KY FAN INEQUALITY

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Abstract. In this note we obtain a new refinement, involving the identric mean of several variables, of the inequality $G_n/G_n' \leqslant A_n/A_n'$, due to Ky Fan.

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