

SHARP INTEGRAL INEQUALITIES FOR C-MONOTONE FUNCTIONS OF SEVERAL VARIABLES

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Abstract. Some sharp integral inequalities for C-monotone functions of several variables are proved. All cases of equality are found and some related results are pointed out and discussed.

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