

MERIT FUNCTION FOR VARIATIONAL-LIKE INEQUALITIES

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Abstract. In this paper, we use the auxiliary principle technique to suggest an iterative method and a merit function for variational-like inequalities. Several special cases, which can be obtained from our results, are also discussed.

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