

ON THE CAUCHY–BUNIAKOWSKY–SCHWARTZ’S INEQUALITY FOR SEQUENCES IN INNER PRODUCT SPACES

S. S. DRAGOMIR

Abstract. In this paper we consider some mappings naturally connected to Cauchy-Buniakowsky-Schwartz’s inequality for sequences of vectors in inner product spaces and point out their main properties. Some applications are also given.

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