ESTIMATING RANDOM POLYNOMIALS BY MEANS OF METRIC ENTROPY METHODS

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Abstract. The purpose of this paper is to indicate how easy, classical metric entropy methods arising from the theory of stochastic processes, apply to get uniform estimates for random polynomials like the well-known Salem-Zygmund's bound [7]. As an application, we give a criterion for uniform convergence of some random Fourier series.

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