

ANALYTIC ISOPERIMETRIC INEQUALITIES

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Abstract. In this paper we introduce the concept of area functions for a given function. We then apply these area functions to establish new analytic and geometric isoperimetric inequalities.

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