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SOME INEQUALITIES FOR COSINE SUMS

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Abstract. We establish sharp lower and upper estimates for the cosine sums $\sum_{k=1}^{n} \frac{\cos k\theta}{k+1}$. We also discuss the possibility of extending these results to other cosine sums of this type.

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