

## PERTURBATION BOUNDS FOR CERTAIN OPERATOR FUNCTIONS

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*Abstract.* Some inequalities for norms and spectral radius involving operator monotone functions have been obtained. Lieb's concavity for trace of certain function has also been considered in general form.

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