

REFINED CONVEXITY AND SPECIAL CASES OF THE BLASCHKE–SANTALO INEQUALITY

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Abstract. We derive the l_p version of the classical Blaschke-Santaló inequality for polar volumes as a consequence of more subtle convexity estimates for the volume of the p -ball in Euclidean space. We also give analogs for the (p, q) -substitution norm.

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