

## ON THE KY FAN INEQUALITY AND RELATED INEQUALITIES I

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*Abstract.* Refinements of the inequalities of Ky Fan [3], Wang and Wang [16], Sándor and Trif [12], and Sándor [14] are obtained. Generalizations and new proofs of some of these inequalities are also included.

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