

SOME NEW INEQUALITIES FOR MOTZKIN NUMBERS

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Abstract. We prove some inequalities which follow from the log-convexity of the sequence of Motzkin numbers M_n and from the log-concavity of the sequence $\frac{M_n}{n!}$.

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