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COMPACT OPERATORS BETWEEN REAL INTERPOLATION SPACES

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Abstract. We show necessary and sufficient conditions for compactness of operators acting between real interpolation spaces.

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