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INEQUALITIES ON POLYNOMIAL ROOTS

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Abstract. The paper presents a survey of inequalities involving roots of univariate polynomials with complex coefficients. These allow improvements in the methods of Bernoulli and Graeffe. Inequalities involving the length of a polynomial are also deduced.

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