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INTEGRAL GENERALIZED MEANS

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Abstract. Generalizing the integral representation of the arithmetic-geometric mean, some authors characterized more means by integrals. In this paper we extend a modified method used by Y.-H. Kim to construct generalized means.

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