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EXTENSIONS OF FATOU'S INEQUALITY

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Abstract. Using some compacity techniques in the space of integrable functions we obtain an expression of the gap in the Fatou's inequality. Also, we derived as corollaries some results of H.-A. Klei.

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