

## ON NEW PROOFS OF WILKER'S INEQUALITIES INVOLVING TRIGONOMETRIC FUNCTIONS

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*Abstract.* In the note, some new proofs for inequalities involving trigonometric functions are given.

*Mathematics subject classification (2000):* Primary 26D05.

*Key words and phrases:* Trigonometric function, Wilker's inequality, Bernoulli number.

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